

Homework: Compare Mie Theory for Spheres with the simple model for absorption below.

Gross Special Purpose Approximation:

$\sigma_{\text{abs}} = a[1 - \exp(-D_{\text{eq}}/\delta)]$. Let $D_{\text{eq}} = v/a$. $\delta = \lambda / (4\pi n_i) = \text{skin depth}$.

$v = 4\pi r^3/3$. $a = \text{average projected area} = \pi r^2$ for a sphere.

$D = 2r$. $D_{\text{eq}} = 2D/3$.

Cases in a 3 matrices for fixed n_r and variable D and n_i :
(calculate the percentage error of the model and Mie theory.)
 $\lambda = 0.5 \text{ } \mu\text{m}$.

$n_r = 1$, $n_r = 1.33$, $n_r = 1.5$

$D = 0.01 \text{ } \mu\text{m}$, $0.1 \text{ } \mu\text{m}$, $1 \text{ } \mu\text{m}$, $10 \text{ } \mu\text{m}$.

$n_i = 0.001$, $n_i = 0.01$, $n_i = 0.1$, $n_i = 1$.

Table for Homework (one for each real refractive index, 1.0, 1.333, and 1.5). Fill each empty table with a percentage error as defined below.

D (microns) → n _i ↓	0.01	0.1	1	10
0.001				
0.01				
0.1				
1				

$$\%Error \equiv 100 \frac{\sigma_{abs}^{Mie} - \sigma_{abs}^{Model}}{\sigma_{abs}^{Mie}} = 100 \frac{Q_{abs}^{Mie} - Q_{abs}^{Model}}{Q_{abs}^{Mie}}$$